

3	Mon. 9/15 Tues 9/16 Wed. 9/17 Fri. 9/19	2.3.1 (rest of) Harmonic Oscillator – algebraic <i>part2</i> 2.3.2 Harmonic Oscillator – analytic (Q10.6) 2.4 Free Particle (Q11)	Daily 3.M Weekly 3 Daily 3.W Daily 3.F
4	Mon. 9/22 Tues 9/23	2.4 Free Particle, Gaussian Wave Packet (problem 2.22 in class)	Daily 4.M Weekly 4

Equipment

- Load our full Python package on computer
- Discrete Finite Well.py & DiscretePIB.py
- Griffith's text
- Moore's text
- Printout of second computational reading.
- Printout of roster with what pictures I have

In general, could we go over an example problem/calculation in class so that we can work through the homework a bit more efficiently?" [Spencer](#)
I agree, I think having another problem to work out would be helpful [Jessica](#)

Could we quickly go over the hermitian conjugate. I understand it in a formulaic sense but going over it quickly could real clear things up with it."

[Kyle B.](#)

"Since we pretty much covered 2.3.1 in class maybe towards the end of class we could get into deriving the recursion formulas in 2.3.2?"

[Casey P.](#)

Daily 3.M Monday 9/15 2.3.1 (rest of) Harmonic Oscillator – algebraic *part2* :

1. *Conceptual*: In words, explain the concept and usefulness of ladder operators.
2. *Conceptual*: What is a hermitian conjugate?
3. *Math*: If you haven't already, finish off numbers 2 and 3 from last Friday.
4. *Math*: In number 4 for last Friday, you got started on one of the weekly problems due tomorrow. You may not yet have worked out part (c) which asks you to find $\langle T \rangle$ and $\langle V \rangle$, but you should be able to answer this question: what do you expect $\langle T \rangle + \langle V \rangle$ to be and why?
5. *Starting Weekly HW*: By now, you should have made a good attempt at all of the weekly HW problems; keep that rolling.

Update for Wednesday's replace $\langle x \rangle$ with $\langle x^2 \rangle$ (otherwise it's trivially 0)

Check dailies

Things we've acquired so far and will use today: Statistical Interpretation

$$|\Psi(x,t)|^2 = \text{Probability Density}$$

$$\langle Q(x,p) \rangle = \int \Psi_n^*(x,t) Q\left(x, \frac{\hbar}{i} \frac{\partial}{\partial x}\right) \Psi_n(x,t) dx$$

$$\hat{p} = \frac{\hbar}{i} \frac{\partial}{\partial x} ()$$

Time-Independent Schrodinger Equation

$$i\hbar \frac{\partial}{\partial t} \Psi(x,t) = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} \Psi(x,t) + V(x)\Psi(x,t)$$

$$\Psi_n(x,t) = \psi_n(x)\varphi_n(t)$$

$$i\hbar \frac{\partial}{\partial t} \varphi_n(t) = E\varphi_n(t) \quad \psi_n(x)E = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} \psi_n(x) + V(x)\psi_n(x)$$

$$\varphi_n(t) = e^{-i\frac{E_n t}{\hbar}}$$

2.3 The Harmonic Oscillator

$$\hat{a}_+ \equiv \frac{1}{\sqrt{2m\hbar\omega}} (-i\hat{p} + m\omega x) \quad \text{and} \quad \hat{a}_- \equiv \frac{1}{\sqrt{2m\hbar\omega}} (i\hat{p} + m\omega x) \quad [\hat{a}_-, \hat{a}_+] = 1$$

$$\hat{H}\psi_n(x) = \frac{1}{2m} (\hat{p}^2 + (m\omega x)^2) \psi_n(x) = \hbar\omega (\hat{a}_- \hat{a}_+ - \frac{1}{2}) \psi_n(x) = \hbar\omega (\hat{a}_+ \hat{a}_- + \frac{1}{2}) \psi_n(x)$$

$$c_n \psi_{n+1}(x) = \hat{a}_+ \psi_n(x) \quad E_{n+1} = E_n + \hbar\omega$$

$$d_n \psi_{n-1}(x) = \hat{a}_- \psi_n(x)$$

$$\psi_0 = \left(\frac{m\omega}{\pi\hbar}\right)^{1/4} e^{-\left(\frac{m\omega}{2\hbar}\right)x^2}$$

$$E_n = \left(n + \frac{1}{2}\right)\hbar\omega \quad \psi_n(x) = \frac{1}{\sqrt{n!}} (\hat{a}_+)^n \psi_{n-1}(x) = \frac{1}{\sqrt{n!}} (\hat{a}_+)^n \psi_0(x)$$